## LOYOLA COLLEGE (AUTONOMOUS), CHENNAI - 600034

## B.Sc. DEGREE EXAMINATION - STATISTICS <br> FIFTH SEMESTER - NOVEMBER 2014 <br> ST 5406 / ST 5404 - ACTUARIAL STATISTICS

Date: 10/11/2014
Time : 09:00-12:00


## Section - A

Answer ALL the questions:
$(10 \times 2=20)$

1. Find the present value at rate of interest of $8 \%$ p.a. of Rs. 250 payable 7 years hence.
2. What is meant by discount rate?
3. What is the effective rate p.a. corresponding to a nominal rate of $8 \%$ p.a. convertible quarterly?
4. Give the relationship between $\mathrm{s}_{\mathrm{n}}$ and $\mathrm{a}_{\mathrm{n}}$.
5. Define : Perpetuity.
6. Show that $i+\frac{1}{s_{n}}=\frac{1}{a_{n}}$
7. What is selection?
8. Explain probabilities of survival and death.
9. Define uniform distribution of deaths.

10 . Write a short note on term insurance.

## Section - B

Answer any FIVE questions:
( $5 \times 8=40$ )
11. Find the value of $(1.03)^{58.4}$.
12. In lieu of a single payment of Rs. 1000 , at the present moment a person agrees to receive 3 equal payments at the end of 3 years, 6 years and 10 years respectively. Assuming a rate of interest of $6 \%$ p.a. what should be the value of each of the 3 payments?
13. Find the amount of an immediate annuity of Rs. 600 p.a. payable twice a year for 15 years on the basis of the nominal rate of $6 \%$ p.a. convertible six times a year.
14. Find the present value of an immediate annuity of Rs. 2400 p.a. payable in equal monthly instalments for 20 years certain at nominal rate of interest of $7 \%$ p.a. convertible half-yearly.
15. Derive the formula for present value of increasing immediate annuity and annuity due.
16. Of two persons $A$ aged (35) and $B$ aged (42), find the probability that
a. A and B both survive 10 years
b. A and $B$ both die within 10 years
c. One of the two lives survives 10 years while the other dies within that period.
17. Explain in detail, the force of mortality.
18. A loan of Rs. $5000 /$ - is to be repaid with interest at $7 \%$ p.a. by means of an immediate annuity for 10 years. Find the level annual payment. What will be the principal outstanding immediately after the $6^{\text {th }}$ payment is made?

## Section - C

## Answer any TWO questions:

19. a) Find the accumulated value of aRs. 500 for a period of 20 years 3 months @ $8 \%$ p.a.
b) Find the present value and accumulated value of an immediate annuity for $n$ years where payments are made at each interval of $r$ years, $n$ being an exact multiple of $r$ and the number of payments being $\mathrm{n} / \mathrm{r}$.
20. a) Calculate the present value of a deferred annuity payable for 10 years certain, the first payment falling due at the end of 6 years from the present time. The annuity is payable at the rate of Rs. 100 p.a. for the first 5 years and Rs. 200 p.a. thereafter.
Given $\left(a_{5}=4.3295, a_{10}=7.7217, a_{15}=10.3797\right)$
b) Find the present value and accumulated value of an annuity due of Rs. 400 p.a. payable in equal quarterly installments for 12 years certain at nominal rate of interest of $8 \%$ p.a. convertible quarterly.
21. a) Three persons are aged $30,35,40$ respectively. Find the probability that
(i) one of them dies before age 45 while the others survive to age 55 .
(ii) at least one of them attains age 65 .
$(10+10)$

$$
(10+10)
$$

b) From the table given below, evaluate ${ }_{3} p_{[21]+1}$ and $d_{1 \mid 2} q_{[20]}$

| AGE AT <br> ENTRY | $\mathbf{I}_{[\mathbf{x}]}$ | $\mathbf{I}_{\mathbf{[ x ] + 1}}$ | $\mathbf{I}_{\mathbf{x}+\mathbf{2}}$ | Age Attained <br> $\mathbf{x + 2}$ |
| :--- | :---: | :---: | :---: | :---: |
| 20 | 495393 | 494534 | 493633 | 22 |
| 21 | 494480 | 493620 | 492716 | 23 |
| 22 | 493566 | 492702 | 491795 | 24 |
| 23 | 492647 | 491781 | 490868 | 25 |

22. a) Find the probability that the survivors of ages ( $x$ ) and years ( $y$ ) will die in the $(t+1)^{\text {th }}$ year.
b) Explain office single premium and annual premium.
